ශී ලංකා විභාග දෙපාර්තමේන්තුව இலங்கைப் பரீட்சைத் திணைக்களம்

අ.පො.ස. (උ.පෙළ) විභාගය/ க.பொ.த. (உயர் தர)ப் பரீட்சை - 2019

නව සහ පැරණි නිර්දේශ/ பුதிய மற்றும் பழைய பாடத்திட்டம்

විෂයය අංකය url இலக்கம்

01

විෂයය பாடம்

භෞතික විදාහව

ලකුණු දීමේ පටිපාටිය/புள்ளி வழங்கும் திட்டம் I පතුය/பத்திரம் I

| පුශ්න අංකය ඛා්ණා ඹුන. | පිළිතුරු අංකය ඛ්කட இல. | පුශ්න අංකය ඛෝණා இන. | පිළිතුරු අංකය ඛාක . මූ න. | පුශ්න අංකය ඛා්ෂා ඉ.න. | පිළිතුරු අංකය விடை இல. | පුශ්න අංකය ඛාශා ඹුන. | පිළිතුරු අංකය ඛානා ය இல. | පුශ්න අංකය ඛෝ னா இல. | පිළිතුරු අංකය ඛ්නා இන. |
|--------------------------------|---------------------------------|------------------------------|----------------------------------------|--------------------------------|------------------------------|-------------------------------|------------------------------------------|--------------------------------------|---------------------------------|
| 01. | 2 | 11. | 4 | 21. | 1 | 31. | 4 | 41. | 2 |
| 02. | 4 | 12. | 4 | 22. | 2 | 32. | 2 | 42. | 2 |
| 03. | 5 | 13. | 3 | 23. | 2 | 33. | 2 | 43. | 3 |
| 04. | 5 | 14. | 5 | 24. | 5 | 34. | 2 | 44. | 2 |
| 05. | 2 | 15. | 2 | 25. | 4 | 35. | 4 | 45. | 4 |
| 06. | 3 | 16. | 4 | 26. | 3 | 36. | 4 | 46. | 4 |
| 07. | 5 | 17. | 1 | 27. | 4 | 37. | 5 | 47. | 2 |
| 08. | 4 | 18. | 3 | 28. | 5 | 38. | 1 | 48. | 4 |
| 09. | 3 | 19. | 5 | 29. | 2 | 39. | 5 | 49. | 4 |
| 10. | 1 | 20. | 4 | 30. | 3 | 40. | 2 | 50. | 3 |

ට විශේෂ උපදෙස්/ விசேட அறிவுறுத்தல் :

චක් පිළිතුරකට/ ඉரு சரியான விடைக்கு 01 ලකුණු බැගින්/புள்ளி வீதம் මුළු ලකුණු/மொத்தப் புள்ளிகள் $1 \times 50 = 50$

1. An experimental setup used in a school laboratory to determine the surface tension of a liquid is shown in figure (1).

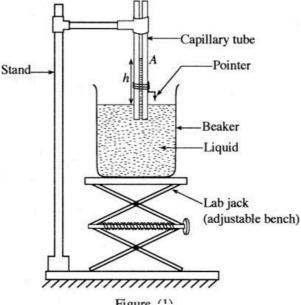
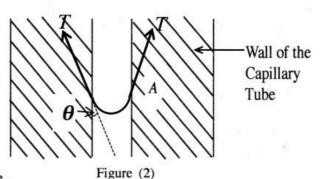


Figure (1)

(a) (i) Figure (2) shows the enlarged view of the vertical cross section of the capillary tube along the axis. Draw the meniscus of the liquid inside the capillary tube and indicate the surface tension T, and the contact angle θ between the liquid and the glass surface of the capillary tube in this figure.



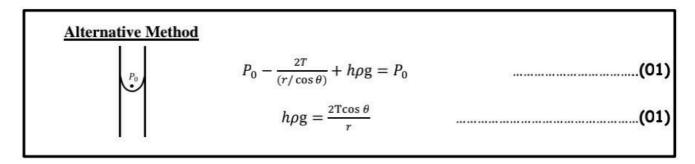
Drawing the meniscus correctly(01) Indicating T (at least one) with an arrow in correct direction(01) Indicating the contact angle θ(01)

(ii) If the height of the liquid column in the capillary tube, the inner radius of the capillary tube, and the density of the liquid are h, r, and ρ , respectively, obtain an expression for $h\rho g$ in terms of T, r, and θ .

$$(2\pi r)T\cos\theta(=mg) = (\pi r^2)h\rho g \qquad \qquad(01)$$

$$h\rho g = \frac{2T\cos\theta}{r} \tag{01}$$

(No Mark only for writing this equation)



| (iii) | Clearly | writing | the | assumption | made, | show | that | the | equation | obtained | in | (ii) | above |
|-------|---------|---------|-----|----------------------|-------|------|------|-----|----------|----------|----|------|-------|
| | can be | reduced | to | $h=\frac{2T}{rog}$. | | | | | | | | | |

The contact angle between the glass and the liquid should be very small or zero.

For small $\theta \to \cos \theta \approx 1$ OR $h\rho g = \frac{2T}{r}$ (01)

(iv) In order to satisfy the assumption mentioned in (iii) above for a given liquid, write down the experimental procedure that should be followed in **the correct order**.

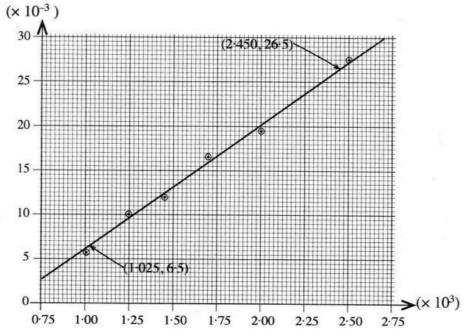
Wash/clean the capillary tube with a <u>base first</u>, then with an <u>acid</u>, and <u>finally</u> with pure <u>water</u>. (Then dry the tube)(02)

(Only for the correct answer with correct order)

(v) Before taking the readings required to determine the height h, what is the adjustment to be made in the experimental setup shown in figure (1)?

Raising the lab jack until the pointer just touches the liquid surface.
.....(02)

(b) The following graph shows the experimental data (in SI units) obtained using 6 capillary tubes with different radii to determine the surface tension of water.



(i) Considering the equation in (a)(iii) above, identify and write down the independent variable (x) and the dependent variable (y) of the graph.

$$x: \frac{1}{r}$$
(01)

| (ii) | Determine | the | surface | tension | of | water | using | the | graph | and | state | the | answer | with |
|------|--------------|-----|---------|---------|----|-------|-------|-----|-------|-----|-------|-----|--------|------|
| | SI units. (I | | | | | | | | 5 50 | | | | | |

Gradient
$$m = \frac{(26.5 - 6.5) \times 10^{-3}}{(2.450 - 1.025) \times 10^{3}} = 1.404 \times 10^{-5} \text{ m}^2$$
(01)

$$n = {}^{2}\text{T}/\rho_g \text{ OR } \text{T} = {}^{m\rho g}/2$$
(01)

$$m = \frac{2T}{\rho g} \frac{0R}{0R} T = \frac{m\rho g}{2}$$

$$\therefore T = \frac{1.404 \times 10^{-5} \times 1000 \times 10}{2}$$
(For the correct substitution).....(01)

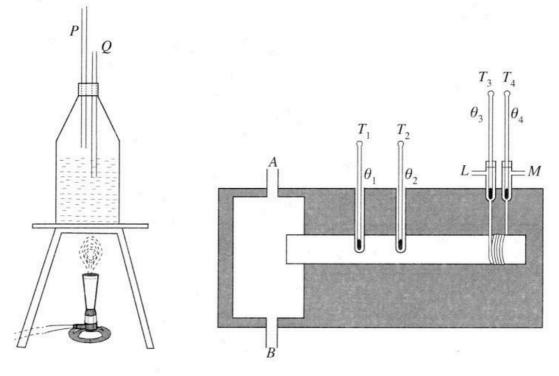
$$T = 7.02 \times 10^{-2} \text{ N m}^{-1} \text{ OR kg s}^{-2} [(7.00 - 7.02) \times 10^{-2}]$$
(02)

(01 Mark for the correct answer and 01 Mark for the correct unit. If only the unit is written without workout, no marks)

- (iii) What would happen to the capillary rise if soap water is used instead of water? Briefly explain the answer.
 - : The capillary rise would be smaller compared to the water when soap water is

The surface tension of water is reduced when soap is added

2. An incomplete diagram of an experimental setup to determine the thermal conductivity of a metal by the Searle's method is shown below.



(a) What are the purposes of inserting tubes P and Q into the steam generator?

P: To supply steam

To control the pressure OR to maintain the pressure inside the steam O: generator at the atmospheric pressure(01)

- (b) Proper connections of steam and water supply to Searle's apparatus are necessary to obtain the accurate result. Accordingly, select each connection and give reasons.
 - (i) Steam supply (A or B):...A(01) Reason:

As steam is less dense than the air, it will fill the chamber before leaving through B OR

If B in connected, steam will leave out through A, without filling the chamber as steam is less dense. Steam should be in contact with the rod throughout the experiment. Condensed water may block B, if it is connected through B To make sure one end of the rod reaches the steam temperature (For any correct reason) (ii) Water supply (L or M):..(01) Reason: To get large difference between the temperatures of the thermometers T₃ and T₄ To ensure the maximum heat absorption by water To achieve the steady state quickly (For any correct reason)(01) (c) State three more measuring instruments needed in this experiment and briefly state the specific measurement taken by each of them. Instrument Measurement Diameter of the ro Separation between T1 and T2 (in Vernier Caliper the rod) Stopwatch Time taken to collect water (at steady state) Electronic/ 3 beam/ Mass of the water collected (at steady state) 4 beam balance Meter Ruler Separation between T_1 and T_2 (in the rod) For any three correct instruments with correct specific Measurement/s......(03) (d) The separation between the thermometers T_1 and T_2 is 8.0 cm. If the constant temperature readings of T_1 and T_2 are 73.8 °C and 59.2 °C, respectively, calculate the temperature gradient. Temperature gradient = $\frac{73.8-59.2}{8\times10^{-2}} = \frac{14.6}{8\times10^{-2}}$(01) = $182.5 \, ^{\circ}\text{C m}^{-1} \, \text{OR} \, 182.5 \, \text{K m}^{-1}$ (01) (e) Does this temperature gradient vary along the rod? Briefly explain the answer. No(01) Because the rod in lagged (Insulated) (f) At thermal steady state, the difference in thermometer readings of T_3 and T_4 is 9.5 °C and the flow rate of water is 120 g per minute. Calculate the rate of heat absorption by water.

Absorption Rate = $\frac{Q}{t} = \frac{ms\theta}{t} \rightarrow \frac{m}{t} \times s \times \theta = \frac{0.12}{60} \times 4200 \times 9.5$ (01)

= 79.77 W (79.8 W)

(Specific heat capacity of water is 4200 J kg-1 K-1.)

| (g) If the cross-sectional area of the metal and state the answer with | ne rod h SI u | is | 12·0 cm ² , calc t. | culate the | thermal of | conductivi | ty of the | |
|-----------------------------------------------------------------------------------------------------------------------------------------------|------------------|-------------|-----------------------------------|--------------------------|--------------------------|--------------------------|------------------|------|
| $Q/_{t} = K.A.\frac{\theta_1 - \theta_2}{l}$ | | | | 2×10^{-4} | × 182.5 | | (| (01) |
| (1 Mark for the correct an | swer a | ano ut | workout, no n | he correct narks. No | et unit. If o mark fo | only the u r the unit | init is wri | tten |
| No. | | | | | | | (| (01) |
| Heat flow through the a | xial d | lir | ection of the OR | rods is | not poss | ible/ not | sufficie | nt |
| Temperature difference measurable | :/grad | die | ent between t | he ther | mometer | s T_1 and | T_2 is not | |
| | | | OR | | | | | |
| Temperature difference | | | (For an | y correct | explanat | ion) | (| |
| A standard spectrometer, a glass the refractive index of the glass. (a) A few necessary adjustment measurements. | s are | to | be done to the | e spectro | meter befo | | | |
| (i) What is the adjustment | that | sh | ould be done t | o the ey | epiece? | | | |
| Eye piece should be adjuste | d to | ob | tain a clear v | iew of t | he cross | wires | | |
| , , | | | 2 | | | | | (01) |
| (ii) Telescope is pointed to the object is formed o | a di | sta | ant object and oss wires. Wha | it is adju t is the p | sted until ourpose of | a clear i this adju | mage of stment? | |
| To receive parallel bean | n/ray: | S (| of light. | | | | | (02) |
| (iii) What is the adjustn | nent t | ha | t should be o | lone to | the slit o | f the col | limator? | |
| The slit should be adjusted source.) | d ot b | e | narrow and v | ertical, | (and illun | | y a light (| |
| (iv) The telescope is broug until a sharp image of of this adjustment? | tht in l | lin slit | e with the colli | mator. The | en the col wires. W | limator is hat is the | adjusted purpose | |
| To obtain a parallel beam/ | rays | of | <u>light</u> from t | he collin | nator/to | | | (02) |
| (b) In order to level the prism to screws P, Q, and R are adjusted | | the | e prism is plac | ed as sh | own in fi | gure (1) | | (02) |
| | | | | Q B Fig | C R ure (1) | | | |

(i) When the telescope is at position T_1 , the screw Qis adjusted to obtain a symmetric image of the slit on the cross wires. When the telescope is moved to the position T_2 , which screw should be adjusted to get a symmetric image of the slit? Screw P(01) (ii) A student stated that the levelling of the prism table could easily be done using a spirit level. Is this statement correct? Briefly explain the answer. No.(01) Prism table should be leveled parallel to the optical axis of the collimator and the telescope, not to level parallel to the horizontal / to the table. Purpose of leveling the prism table is to make it parallel to the light beam of the collimator and the telescope, not to the horizontal. Leveling the prism table parallel to the horizontal will not make it parallel to the light beam of the collimator and the telescope. (For any correct explanation)(01)

(c) When the telescope is at positions T_1 and T_2 , the readings of the spectrometer are 279° 58' and 38° 02', respectively. Note that the telescope passes the zero of the main scale when it is moved from T_1 to T_2 . Calculate the prism angle A.

$$2A = 360^{\circ} - T_1 + T_2 = 360^{\circ} - 279^{\circ} 58' + 38^{\circ} 02'$$

= 118° 04'
 $A = 59^{\circ} 02'$ (01)

(d) To determine the angle of deviation of a light ray by the given glass prism, a student measured the incident and emergent angles i_1 and i_2 , respectively, as shown in figure (2). The graph shows the variation of i_2 with i_1 .

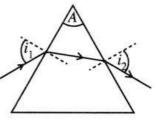
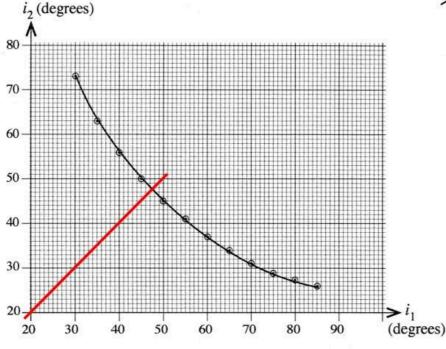


Figure (2)



(i) Write down an expression for the angle of deviation d, in terms of the prism angle A, and the angles i_1 and i_2 .

$$d = (i_1 + i_2) - A$$
(02)

(ii) Determine the minimum angle of deviation D by using the graph.

From the graph $i_1 = i_2 = i$ OR Correct line as indicated in the graph(01)

$$i = 47.5^{\circ}$$
 OR $47^{\circ} 30'$ OR 47° OR 48° (01)

Minimum angle of deviation $\Rightarrow D = 2i - A$ (01)

$$= 2 \times (47.5^{\circ}) - 59^{\circ}02'$$
(01)

$$= 35^{\circ} 58' (34^{\circ} 58' \text{ OR } 36^{\circ} 58') \dots (01)$$

(iii) Calculate the refractive index of the glass that the prism is made of.

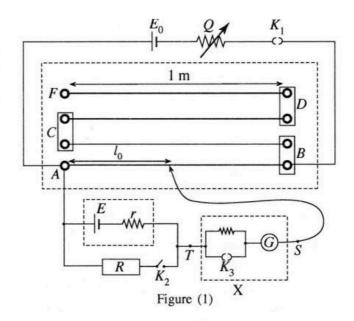
$$n = \frac{\sin(\frac{A+D}{2})}{\sin(\frac{A}{2})} = \frac{\sin(\frac{59^{\circ}02'+35^{\circ}58'}{2})}{\sin(\frac{59^{\circ}02'}{2})}$$
 (01)

Alternative method

$$n = \frac{\sin t}{\sin r} = \frac{\sin 47^{2} \text{ 30}}{\sin 29^{\circ} \text{ 31}'} \tag{01}$$

$$= 1.49 \quad (1.48 - 1.51) \tag{01}$$

4. Figure (1) shows an experimental setup of a potentiometer with a 4m long wire, that can be used to determine the internal resistance r of a given cell with electromotive force (emf) $E (< E_0)$.



Range can be adjusted by varying the value of Q

increasing/varying the length of the potentiometer wire(01

(c) A student observed a small deflection of the galvanometer even when there is no current passing through it. Is it advisable to use this galvanometer for this experiment? Give reasons for the answer.

Yes. (01)

OR

Zero error of the galvanometer does not affect the result of the experiment OR

It is the deflection, not the zero reading of the galvanometer that matters in the experiment. OR

Experiment can be continued by observing the deflection from the initial position. (For any correct reason)......(01)

(d) When the switch K_2 is open, the balance length of the potentiometer wire is l_0 . When K_2 is closed, the balance length is l. Obtain an expression for the internal resistance r of the given cell in terms of l, l_0 , and R.

$$E = kl_0$$

$$V = kl$$

$$OR \quad \frac{V}{E} = \frac{l}{l_0}$$

$$V = E\left(\frac{R}{R+r}\right) \quad OR \quad \frac{V}{E} = \frac{R}{R+r}$$

$$\therefore \frac{R}{R+r} = \frac{l}{l_0}$$

$$r = R\left(\frac{l_0}{l} - 1\right)$$
(01)

(e) With the given potentiometer, the balance length can be measured with a maximum error of 1 mm. If $R = 8 \Omega$, $l_0 = 72.4 \,\mathrm{cm}$ and $l = 50.1 \,\mathrm{cm}$, calculate the maximum value that could be obtained for the internal resistance r.

$$l_0 = 72.4 + 0.1 \text{ cm}$$
 OR $l = 50.1 - 0.1 \text{ cm}$ (01)
 $r = 8 \times \left(\frac{72.4 + 0.1}{50.1 - 0.1} - 1\right) = 8 \times \left(\frac{72.5}{50.0} - 1\right)$ (01)
 $= 3.55 \Omega$ OR 3.60Ω (01)

(f) Internal resistance r can be determined more accurately by a graphical method. Considering R as a variable resistor, rearrange the equation obtained in (d) to plot a suitable graph. Write down the independent (x) and dependent (y) variables of the graph.

$$r = R\left(\frac{l_0}{l} - 1\right)$$

 $\frac{l_0}{l} = (r)\frac{1}{R} + 1$ OR $\frac{1}{l} = \left(\frac{r}{l_0}\right)\frac{1}{R} + \frac{1}{l_0}$ (01)

- (g) The potentiometer circuit shown in figure (1) can be modified by replacing the part of the circuit marked X in figure (1), by the circuit shown in figure (2). For this, the terminals S' and T' of the circuit shown in figure (2) are connected respectively to points S and T of the potentiometer circuit shown in figure (1).
- S'

 Green

 LED

 Figure (2)

(i) Assume that the balance point is located between A and B in the modified circuit.

What is the colour of the Light Emitting Diode (LED) which is lit when the sliding key is placed at A and B?

(ii) Briefly explain how the balance point could be found using the modified circuit.

When the sliding key is kept at different points along the potentiometer wire, at the balance point both LEDs should not illuminate

OR

When the sliding key is kept at different points along the potentiometer wire, at the balance point LEDs light ON and OFF, alternately.

(02)

- (iii) State **two** advantages of this modified circuit in finding the balance point, when compared with the circuit shown in figure (1).
 - Balance point can be determined with high accuracy (due to the very high sensitivity of the circuit)
 - No current passes through the points S and T even when the potentiometer is not balanced.
 - · Cell discharges slowly.
 - Rough balancing of the potentiometer can be avoided.

(For Any two correct answers, 1 Mark for each)(02)

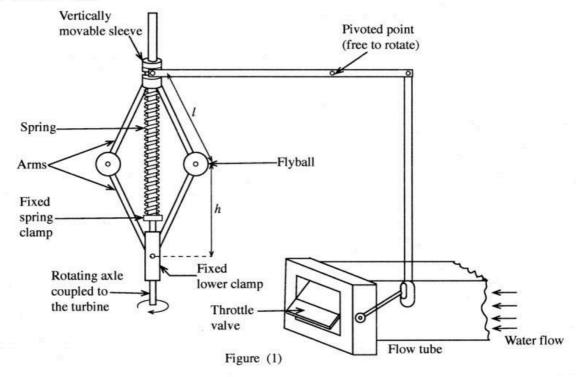
5. (a) In electric power generators, the frequency of the output voltage depends on the number of magnetic poles P and the number of revolutions per minute N of the generator. The frequency f in Hz is given by

$$f = \frac{P \times N}{120} .$$

A portable generator consisting of two magnetic poles typically works at 3000 revolutions per minute (rpm).

Find the following:

- (i) The frequency of the output voltage of the generator
- (ii) The rotational speed of the generator in radians per second (rad s⁻¹) (Take $\pi = 3$)
- (b) A student has designed a model of a hydro-power plant by replacing the engine of the portable generator mentioned in (a) above, with a turbine that can be rotated by a water flow. He observed that the frequency of the output voltage varies with the consumption of electricity even at a constant water flow. To control the frequency variation of the output, he designed a controlling device to adjust the water flow to the turbine. Schematic diagram of the controlling device connected to a throttle valve is shown in figure (1).



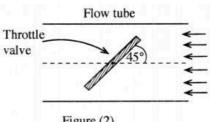
Assume all the joints in this device are free to move without friction. During the rotation, flyballs move horizontally and it makes the sleeve move up and down along the rotating axle. This device is symmetric about the rotating axle. Opening and closing of the throttle valve is automatically controlled by the rotational speed of the turbine. All the other parts of the device can be assumed to be massless except the flyballs.

- (i) Draw the free body force diagram for a flyball assuming each arm connected to it, is under tension. Consider the mass of a flyball to be m.
- (ii) If the angular velocity of each flyball about the rotational axle is ω rad s⁻¹, show that the tensions in the upper and lower arms are respectively given by $\frac{ml}{2} \left(\omega^2 + \frac{g}{h} \right)$ and $\frac{ml}{2} \left(\omega^2 \frac{g}{h} \right)$.

Here l is the length of each arm and h is the height to each flyball from the lower clamp.

- (iii) When the frequency of the output voltage is 50 Hz, the value of h is 30 cm. Show that the contribution to the tension from the term $\frac{g}{h}$ can be neglected.
- (iv) If m = 1 kg and l = 50 cm, calculate the tension in an upper arm.
- (v) When the frequency of the output voltage is 50 Hz, the contraction of the spring is 20 cm. Determine the spring constant of the spring.

(c) When the frequency of the output voltage is 50 Hz, the throttle valve is set to block 50% of the flow. That is, the valve is making an angle of 45° with the axis of the flow tube as shown in figure (2). Assume that the closing of the throttle valve is proportional to the angle of the valve with the axis of the tube.



The frequency of the output voltage depends on the consumption of electricity. When the consumption increases, the output frequency decreases and vice versa.

Figure (2)

- (i) According to the design, when the frequency of the output voltage becomes 25 Hz, the throttle valve will be fully opened. The valve will remain fully open even for frequencies lower than 25 Hz. Determine the following at the instant of fully opening the throttle valve. (Neglect the contribution from the term $\frac{g}{h}$)
 - (1) Tension of an upper arm
 - (2) Contraction of the spring
- (ii) When the frequency of the output voltage increases, the throttle valve closes gradually to decrease the flow rate. If the flow is to be blocked by 75%, what should be the frequency of the output voltage?

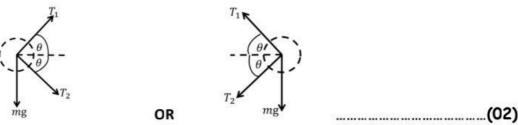
(a) (i)
$$f = \frac{3000 \times 2}{120} = 50 \text{ Hz}$$
 (01)

(Substitution should be there to award this mark)

(ii) Rotational speed of the generator (taking $\pi = 3$)

$$\omega = 2\pi f = 2 \times 3 \times 50 \text{ OR } \omega = \frac{3000}{60} \times 2\pi = \frac{3000}{60} \times 2 \times 3$$
(01)
= 300 rad s⁻¹

(b) (i)



(01 Mark for mg being vertical and 01 Mark for tensions with any labeling. If there is a clearly identifiable difference in angles, deduct 01 mark)

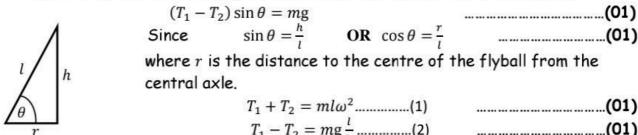
(ii) For the 1st free body force diagram (or the relevant diagram)

Applying Newton's 2^{nd} law (F = ma) along \rightarrow direction

$$(T_1 + T_2)\cos\theta = mr\omega^2 = m\frac{v^2}{r}$$
(02)

(01 Mark for LHS and 01 Mark for RHS, To award this mark, instead of r, any other symbol can be used)

Considering the forces along \(\) direction for the equilibrium of the flyball



$$T_{1} + T_{2} = ml\omega^{2}.....(1) \qquad (01)$$

$$T_{1} - T_{2} = mg\frac{l}{h}....(2) \qquad (01)$$

$$(1) + (2) \Rightarrow T_{1} = \frac{ml}{2} \left[\omega^{2} + \frac{g}{h}\right]$$

$$(1) - (2) \Rightarrow T_1 = \frac{2}{2} \left[\omega + h \right]$$

$$(1) - (2) \Rightarrow T_2 = \frac{ml}{2} \left[\omega^2 - \frac{g}{h} \right]$$

(iii) When the generator operates at 50 Hz, the rotational speed

$$\omega = 300 \text{ rad s}^{-1}$$
, and $h = 30 \text{ cm}$.

: Therefore, $\omega^2 = (300)^2 = 90000 \text{ s}^{-2}$

$$\frac{g}{h} = \frac{10}{30 \times 10^{-2}} = 33.3 \text{ s}^{-2}$$
 (01)

$$\therefore \frac{g}{h} \ll \omega^2$$
 (For the comparison of two correct values)(01)

Therefore, the term g/h can be neglected when determining the tensions T_1 and T_2 .

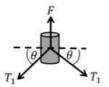
(iv) Tension in an upper arm

$$T_{1} = \frac{ml}{2} \left[\omega^{2} + \frac{g}{h} \right] \approx \frac{ml\omega^{2}}{2}$$

$$= \frac{1 \times 50 \times 10^{-2} \times (300)^{2}}{2}$$

$$= 22500 \text{ N} \qquad [(2.25 - 2.50) \times 10^{4} \text{N}] \qquad (01)$$

(v) When the sleeve is in equilibrium, the spring force on the sleeve is balanced by the tensions in two upper arms as below.



When the compression of the spring (say x) is 20 cm, the spring force

$$F = kx$$
 (01)
= $2T_1 \sin \theta = 2T_1 \frac{h}{l}$ (01)

where k is the spring constant.

(To award this mark above free body force diagram can also be considered)

$$k \times 20 \times 10^{-2} = 2 \times 22500 \times \frac{30 \times 10^{-2}}{50 \times 10^{-2}}$$
(01)

$$k = 1.35 \times 10^5 \text{ Nm}^{-1} [(1.35 - 1.50) \times 10^5 \text{ Nm}^{-1}]$$
(01)

(c) (i) (1) When the frequency is f=25 Hz, the rotational speed of the generator is $\omega=\frac{300}{2}=150$ rad s⁻¹(01)

Tension in the upper arm

$$T_1 = \frac{ml\omega^2}{2}$$

$$= \frac{1 \times 50 \times 10^{-2} \times (150)^2}{2}$$

$$= 5625 \text{ N} \qquad [(5.6 - 6.2) \times 10^3 \text{ N}] \qquad (01)$$

(2) When the sleeve moves up by a distance (say d), the throttle valve opens. Then, the contraction (say e) of the spring becomes,

$$e = x - d = 20 - d$$
(01

The height (h) to the flyball from the fixed lower clamp becomes,

$$h = 30 + d/2$$
(01)

Now for the equilibrium of the sleeve

$$F = ke = 2T_1 \sin \theta = 2T_1 \frac{h}{l}$$

$$1.35 \times 10^5 \times (20 - d) \times 10^{-2} = 2 \times 5625 \times \frac{(30 + d/2) \times 10^{-2}}{50 \times 10^{-2}}$$
 (for the substitution)......(01)

$$d = 13.84 \text{ cm}$$
 (13.8 cm)

Therefore, the contraction of the spring = 20 - 13.84 cm= 6.16 cm [6.1 - 6.2 cm](01)

Alternative Method

When the frequency is 50 Hz,

the length of the spring =
$$2h - h_o = 2 \times 30 - h_o = (60 - h_o)$$
 cm(01)

The natural length of the spring =
$$20 + (60 - h_o) = (80 - h_o)$$
 cm(01)

When the frequency becomes 25 Hz, let the contraction of the spring be e(say) in cm.

Then the length of the spring =
$$(80 - h_{\theta}) - e = 2h' - h_{\theta}$$
(01)

$$F = kx = 2T_1 \frac{h'}{l}$$

$$1.35 \times 10^5 \times e = 2 \times 5625 \times \frac{(80-e)/2}{50 \times 10^{-2}}$$
(01)

$$e = 6.15 \text{ cm}$$
 [6.1 - 6.2 cm](01)

(ii) When the frequency is 50 Hz, throttle valve is 50% closed, and becomes fully open (i.e. 0% closed) when the frequency becomes 25 Hz.

Therefore, for the closing of the throttle valve changes by 50% when the frequency change is (50 - 25)Hz = 25 Hz.(01)

Therefore, the frequency to block the throttle valve by 75% (i.e. to increase the closing by 25%) $f = 50 + \frac{25 \times 25\%}{50\%} = 50 + \frac{25}{2}$ (01)

Alternative Method

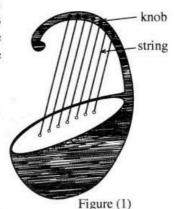
When the frequency is 50 Hz, throttle valve is 50% closed, i.e. throttle valve makes an angle of 45° with the axis of the tube. When the frequency becomes 25 Hz, it becomes fully open, i.e. the throttle valve become parallel with the axis of the tube. Therefore, when the frequency is reduced by 25 Hz (from 50 Hz to 25 Hz), the change in the angle of the throttle valve with the axis of the tube is 45°(01)

To block the throttle valve by 75%, the angle should be increased by $\frac{45^o}{2}=22.5^o$ from $45^o.$ Therefore the frequency to block the throttle valve by 75%

$$f = 50 + \frac{25 \times 22.5^{o}}{45^{o}}$$
(01)
= 62.5 Hz(01)

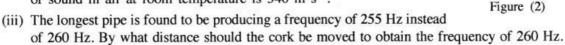
- 6. (a) (i) Draw the standing wave patterns of the fundamental mode and the first two overtones produced by a vibrating stretched string, in three separate diagrams. Mark the nodes as 'N' and the antinodes as 'A' in the diagrams. (Neglect end corrections.)
 - (ii) Obtain an expression for the frequency f_n of the nth harmonic in terms of n, T, l, and m, where T is the tension, l is the length, and m is the mass per unit length of the string.
 - (iii) For a given string, state two possible ways of changing the harmonic frequencies.
 - (b) A harp like musical instrument shown in figure (1) consists of 7 identical stretched strings with different lengths. The longest string of length l_1 , produces the musical note 'C' (ϖ, ϖ) with the fundamental frequency of 260 Hz. The corresponding lengths of the strings which produce all the musical notes are given in the table as fractions of l_1 .

| | ස | 8 | ဖ | 9 | ප | ۵ | නි |
|------------------|------|------|------|------|------|------|------|
| Musical Notes | С | D | Е | F | G | Α | В |
| riotes | സ | ரி | க | ш | U | த | நி |
| $\frac{l}{l_1}$ | 1.00 | 0.89 | 0.79 | 0.70 | 0.67 | 0.59 | 0.53 |

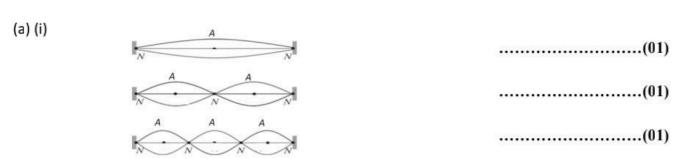


Cork

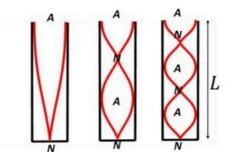
- (i) If all the strings are under the same tension, calculate the fundamental frequencies of musical notes 'F'(②, ɒ) and 'B' (名, 禹).
- (ii) To obtain a correct musical note, the frequency can be fine tuned by adjusting the tension of the string. By what percentage should the tension of the string be adjusted to change the frequency by 1%?
- (c) A student designs and builds a set of panpipes to produce musical notes given in the above table, by using narrow PVC pipes with different lengths as shown in figure (2). Lower end of all the pipes are closed with corks.
 - (i) Draw the standing wave patterns of the fundamental mode and the first two overtones produced by a one end closed pipe of length L, in three separate diagrams. Mark the nodes as 'N' and the antinodes as 'A' in the diagram. (Neglect end corrections.)
 - (ii) Calculate the required lengths of the pipes in cm, which produce the musical notes 'C'(\mathfrak{S} , \mathfrak{m}) and 'B' (\mathfrak{S} , \mathfrak{g}). Assume that the velocity of sound in air at room temperature is 340 m s⁻¹.



(iv) If the cork fell completely out of a pipe, what would happen to the fundamental frequency produced by the pipe? Justify the answer with a suitable diagram.



(Atleast one of the diagrams should have 'A' & 'N', if not deduct 01 Mark.
For different lengths of the string deduct 01 Mark)



(Atleast one of the diagrams should have 'A' & 'N', if not deduct 01 Mark. Deduct 1 Mark if lengths of the tubes are different)

| (01) |
|-----------------------|
| (01) |
| of frequency |
| (01) |
| of frequency |
| |
| (01) |
| (01) |
| (01) |
| (01) |
| (01) |
| nsed(01) |
| (01) rect diagram) |
| |

- 7. When an object is falling through a viscous medium, it is subjected to the buoyant force and the drag force. The buoyant force pushes the object upward while the drag force acts against the motion of the object with respect to the medium.
 - (a) The drag force for a solid spherical object falling in a liquid medium can be expressed by the Stokes'
 - (i) Write down the Stokes' formula for a solid spherical object and name the parameters.
 - (ii) Write down two assumptions that are used in deriving the Stokes' formula.
 - (b) Consider an air bubble rising gradually upward in a viscous fluid. Stokes' Law can be applied to determine the time taken by an air bubble to reach the surface of the fluid. Neglecting the effect of the pressure change with height, the instantaneous velocity V(t) of an air bubble in a viscous medium at a given time t can be given by

 $V(t) = V_T \left(1 - e^{-\frac{t}{\tau}}\right)$, where V_T and τ are the terminal velocity and the relaxation time of the motion of the air bubble, respectively.

- (i) If the relaxation time for the motion of an air bubble in a viscous medium is 4 μs, calculate the time it takes for the instantaneous velocity to be 50% of V_T from the rest (Take $\ln 0.5 = -0.7$)
- (ii) Calculate the time taken by the air bubble to increase the instantaneous velocity from 50% to 90% of V_T . (Take $\ln 0.1 = -2.3$)
- (iii) Considering the answers obtained in (b)(i) and (b)(ii) above, plot the variation of the instantaneous velocity of the air bubble as a function of time. Clearly indicate V_T on the graph.
- (c) Consider an air bubble rising from the bottom of an oil tank which is filled upto 10 m height.
 - (i) Obtain an expression for the resultant force acting on the air bubble in terms of η , ρ_o , ρ_a , a, and v, where η is the coefficient of viscosity of oil, ρ_o is the density of the oil, ρ_a is the density of air, a is the radius of the air bubble, and v is the velocity of the air bubble.
 - (ii) It is given that $\eta = 7.5 \times 10^{-2}$ Pa s, $\rho_0 = 900$ kg m⁻³, $\rho_a = 1.225$ kg m⁻³, and the average radius of an air bubble a = 0.1 mm. Neglecting the weight of the air bubble, and the effect due to the variation of pressure with height, calculate the terminal velocity of the air bubble.
 - (iii) Calculate the radius of the air bubble just below the surface of the oil, if the internal pressure of the bubble is 100.33 kPa, atmospheric pressure is 100 kPa, and the surface tension of oil is $2.0 \times 10^{-2} \text{ N m}^{-1}$.
 - (iv) Considering the change in radius of the air bubble with height, sketch the variation of its instantaneous velocity with time.

(a) (i)
$$F = 6\pi \eta a v$$
(02)

 η - Coefficient of viscosity

a - Radius of the sphere

v - Velocity of the sphere

(ii) Flow is streamline with respect to the object

Surface of the object is smooth

No interaction with other objects/ Infinite large area around the object.

The temperature of the fluid is constant

Made of homogeneous material

Fluid must be at rest (For any two assumptions with 01 Mark each)......(02)

(b) (i)
$$V(t) = V_T \left(1 - e^{-t/\tau} \right)$$

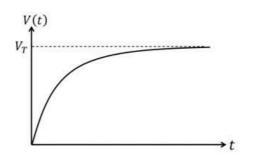
$$50 \% V_T = V_T (1 - e^{-t/\tau}) \Rightarrow 1 - e^{-t/\tau} = 0.5$$
 (01)

$$\Rightarrow e^{-t/\tau} = 0.5 \Rightarrow -t/\tau = \ln 0.5 = -0.7$$

$$t = 0.7 \times \tau = 0.7 \times 4 \times 10^{-6} = 2.8 \times 10^{-6} \text{ s}$$
(No marks allocated)

(ii)
$$90 \% V_T = V_T \left(1 - e^{-t/\tau} \right) \Rightarrow 1 - e^{-t/\tau} = 0.9$$
(01)
$$e^{-t/\tau} = 0.1 \Rightarrow -t/\tau = \ln 0.1 = -2.3$$
(01)
$$t = 2.3 \times \tau = 2.3 \times 4 \times 10^{-6} \text{ s} = 9.2 \times 10^{-6} \text{ s}$$
(No marks allocated)

(iii)



(01 Marks for the shape of the graph, and 01 Mark for marking the axis, 01 mark for indicating V_T)

(c) (i) Forces acting on the air bubble are buoyant force (up thrust) ↑, drag force ↓, and weight of the air bubble 1.

The resulting force on the air bubble along † direction

$$F_R = V \rho_o g - 6\pi \eta a v - V \rho_a g \qquad \qquad (\textbf{O3})$$

$$(\textbf{For each correct term with correct sign: 01 Mark})$$

$$= \frac{4}{3}\pi a^3 \rho_o g - 6\pi \eta a v - \frac{4}{3}\pi a^3 \rho_a g \qquad (\textbf{O1})$$

(ii) When the terminal velocity is achieved, $F_R = 0$ Neglecting the weight (i.e. $\frac{4}{3}\pi a^3 \rho_a g$) of the air bubble and the effect due to the variation of pressure with height (i.e. no change in volume)

$$6\pi \eta a v_T = \frac{4}{3} \pi a^3 \rho_o g \implies v_T = \frac{2}{9} \frac{\rho_o g}{\eta} a^2$$
 (02)

$$av_T = \frac{1}{3}\pi a^3 \rho_0 g \Rightarrow v_T = \frac{1}{9}\frac{100}{\eta} a^2$$

$$v_T = \frac{2}{9} \times \frac{(900) \times 10}{7.5 \times 10^{-2}} \times (0.1 \times 10^{-3})^2$$
(01)

$$= 2.67 \times 10^{-4} \text{ m s}^{-1} \quad [(2.6 - 2.7) \times 10^{-4} \text{ m s}^{-1}] \dots (01)$$

(iii) The difference in pressure of the air bubble inside and outside

$$\Delta P = P_{\text{inside}} - P_{\text{outside}} = \frac{2T}{r}$$
 (02)

(01 Mark each for each side of the equation)

$$(100.33 - 100) \times 10^3 = {}^{2 \times (2 \times 10^{-2})}/r$$
(01)

(iv) The terminal speed $v_T \propto a^2$, therefore v_T increases as the radius of the air bubble a increases. But due to the pressure variation with height, the volume of the air bubble increases and therefore a increases. Due to this continuous variation of a, the air bubble accelerates without achieving the terminal speed.



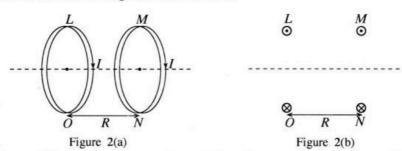
(1 mark for axis labeling, 1 mark for behavior of initial rising, and the 1 mark is for later, continuous slow rise)

- 8. (a) (i) A current I flows through a thin wire of very small length Δl . Show that the magnetic flux density ΔB at a point with a perpendicular distance d away from this wire, is given by $\frac{\mu_0 I \Delta l}{\sqrt{l^2}}$.
 - (ii) A current I flows through a flat circular coil of radius R with N number of turns as shown in figure (1). Obtain an expression for the magnitude of the magnetic flux density B at the centre of the coil.



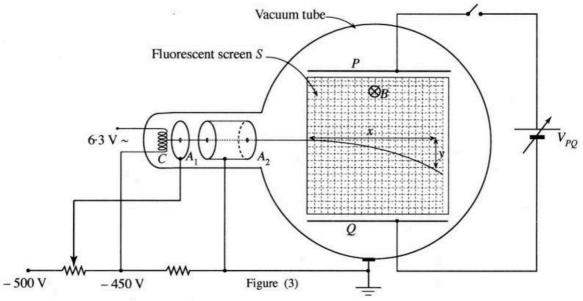
(iii) Two such coils are placed coaxially with a separation R as shown in figure 2(a). The current I flows through both coils in the same direction. Figure 2(b) shows the vertical cross section of the coils through the common axis.



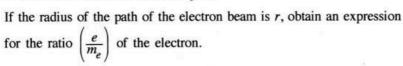


Copy the figure 2(b) onto the answer script and draw the magnetic field lines to illustrate the magnetic field due to both coils.

(b) The apparatus shown in figure (3) can be used to determine the charge to mass ratio $\left(\frac{e}{m_e}\right)$ of an electron. The vacuum tube has a filament cathode C, electrodes A_1 and A_2 , and a vertical fluorescent screen S with grid lines. The path of the electron beam can be seen on the fluorescent screen.



- (i) The function of the electrode A_1 is to control the intensity of the electron beam. What is the function of the electrode A_2 ?
- (ii) If a negative voltage (-V) is applied to electrode A_1 , obtain an expression for the speed of an electron travelling through the electrode A_2 . (Charge of an electron is -e and mass of an electron is m_e .)
- (iii) The spherical part of the tube is placed between two flat circular coils carrying the same current as shown in figure (4). Thereby a uniform magnetic field B is applied perpendicularly to the screen S. This makes the electrons move in a circular path.



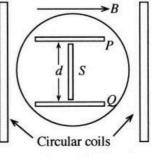


Figure (4)

- (c) A dc voltage can be applied between two parallel metal plates P and Q as shown in figure (3). The plates P and Q are separated by a distance d as shown in figure (4). While the magnetic field B is applied, the potential difference between the plates V_{PQ} can be adjusted until there is no deflection of the electron beam. This process can be utilized as an alternative way to determine the speed of the electrons.
 - (i) Draw the electric and magnetic forces acting on an electron within the plates P and Q, after the above adjustment is done.
 - (ii) Obtain an expression for the speed of the electrons in terms of d, B and V_{PO} .
 - (iii) When B = 1 mT and $V_{PO} = 0$, the radius of the path of the electrons is 6 cm. When V_{PO} = 840 V, there is no deflection of the electron beam. The separation between the plates P and Q is 8 cm.

Calculate

- (1) the speed of an electron, and
- (2) the charge to mass ratio $\left(\frac{e}{m_a}\right)$ of an electron.
- (a) (i) From Biot-Savart Law

 ΔB

$$\Delta B = \frac{\mu_0 I \Delta l}{4\pi d^2} \sin \theta \qquad \qquad (01)$$

$$\Delta B = \frac{\mu_0 I \Delta l}{4\pi d^2} \sin\left(\frac{\pi}{2}\right) \tag{01}$$

$$\Delta B = \frac{\mu_0 I \Delta l}{4\pi d^2}$$

(ii) Magnetic flux density at the centre of the coil due to Δl ,

$$\Delta B = \frac{\mu_0 I \Delta l}{4\pi R^2} \tag{01}$$

Magnetic flux density at the <u>centre</u> due to <u>whole coil</u>, $B = \sum \Delta B$ $B = \sum \frac{\mu_o}{4\pi} \frac{I\Delta l}{R^2} \qquad \mathbf{OR} \qquad B = \frac{\mu_o}{4\pi} \frac{l}{R^2} \sum \Delta l$

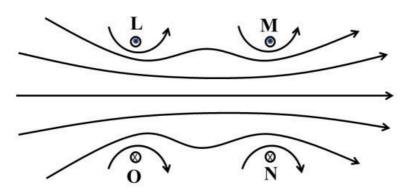
$$B = \sum \frac{\mu_o}{4\pi} \frac{I\Delta l}{R^2}$$

OR
$$B = \frac{\mu_0}{4\pi} \frac{1}{R^2} \sum \Delta$$

$$B = \frac{\mu_0}{4\pi} \frac{I}{R^2} (2\pi RN)$$
 (02)

$$B = \frac{\mu_0 IN}{2R}$$
 (1 Mark for $2\pi R$ and 1 Mark for multiplying by N)
.....(01)

(iii)



At least 2 nearly parallel lines close to the centre of the coils(01)

Arrow/s in a central line/s of force in correct direction(01)

Additional symmetric lines with arrow/s of force on the same coil(01)

(b)(i) Accelerating electrons (towards A₂) OR Producing a collimated beam of high velocity electrons(02) (ii) Kinetic Energy + Potential Energy at $A_1 = K.E. + P.E.$ at A_2

Considering the conservation of energy

OR For any correct reasoning(01)

$$0 + (-e)(-V) = \frac{1}{2}m_e v^2 + 0 \qquad (02)$$

(1 Mark each for writing each side of the equation)

$$v^{2} = \frac{2eV}{m_{e}}$$

$$v = \sqrt{\frac{2eV}{m_{e}}}$$
(01)

Alternative Method

If the distance between the two anodes is l, and the electric field between the two anodes is E, the force on an electron $F_e = eE$

$$m_e a = e \left(\frac{V}{I} \right)$$
(01)

$$\therefore a = \frac{eV}{lm_a}$$
 (01)

Using
$$v^2 = u^2 + 2as$$

$$v^2 = 0 + 2\left(\frac{eV}{lm_e}\right)l$$
(01)

$$v = \sqrt{\frac{2eV}{m_e}} \tag{01}$$

(iii) For circular motion of an electron;

Centripetal force = force on an electron due to magnetic field

$$\frac{m_e v^2}{r} = Bev \tag{02}$$

(1 Mark each for each side of the equation)

$$v = \frac{Ber}{m_e}$$

$$\therefore \frac{Ber}{m_e} = \sqrt{\frac{2eV}{m_e}} \quad \mathbf{OR} \quad \left(\frac{Ber}{m_e}\right)^2 = \frac{2eV}{m_e} \tag{01}$$

(c)(i)

$$F_{E} \text{ OR } eE$$

$$----e \longrightarrow v$$

$$F_{E} \text{ OR } evB$$

$$(01)$$

(E is the Electric Field Intensity between the plates, P and Q)

(ii) For no deflection of electrons: $F_B = F_E$

$$Bev = eE$$
(01)

$$Bev = e\left(\frac{V_{PQ}}{d}\right) \tag{01}$$

$$v = \frac{V_{PQ}}{Rd} \tag{01}$$

$$v = \frac{V_{PQ}}{Bd} \tag{01}$$

(iii) (1)
$$v = \frac{v_{PQ}}{^{Bd}}$$

$$= \frac{^{840}}{^{(1\times10^{-3})\times(8\times10^{-2})}}$$

$$v = 1.05 \times 10^7 \text{ m s}^{-1}$$
(01)

(2) For circular motion of an electron

$$Bev = \frac{m_e v^2}{r}$$

$$\frac{e}{m_e} = \frac{v}{Br}$$

$$= \frac{1.05 \times 10^7}{(1 \times 10^{-3}) \times (6 \times 10^{-2})}$$

$$= 1.75 \times 10^{11} \text{ C kg}^{-1}$$
(01)

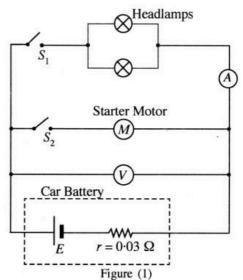
9. Answer either part (A) or part (B) only.

Part (A)

- (a) The electromotive force (emf) of an electric source is defined as the work done by the source on a unit charge. Using this definition;
 - (i) determine the units of emf.
 - (ii) obtain an expression for the power generated by a source in terms of its emf E and the current I flowing through it.
- (b) A source of emf E and internal resistance r is connected to an external resistor with resistance R. Obtain an expression for the total energy dissipated in the circuit in time t, in terms of E, r, R, and t.
- (c) Consider an electrochemical battery of a car that powers the starter motor and the headlamps as shown in the circuit of figure (1). Rated power of each headlamp is 60 W. The internal resistance of the battery is 0.03 Ω . Consider that the ammeter behaves as an ideal ammeter.

When only the headlamps are turned on $(S_1 \text{ is closed})$ without starting the car $(S_2 \text{ is open})$, the voltmeter shows a value of 12.0 V.

- (i) What is the reading of the ammeter?
- (ii) What is the resistance of a headlamp?
- (iii) Calculate the emf of the battery.



- (d) When the starter motor is just turned on $(S_2$ is just closed) while the headlamps are ON, the ammeter shows a value of 8.0 A. Calculate,
 - (i) the current through the starter motor, and
 - (ii) the resistance of the starter motor.
- (e) When the armature of the starter motor is rotating while the headlamps are ON, the current through the starter motor is 34·2 A and the voltmeter reading is 11·0 V.
 Calculate,
 - (i) the back emf, and
 - (ii) the efficiency of the starter motor, at this instant.
- (f) Sketch the variation of the back emf E_b of the motor with the current flowing through it.
- (g) The battery discharged considerably because the driver parked the car without turning off the headlamps on a certain night. As a result, emf of the battery dropped to 10·8 V and its internal resistance increased to 0·24 Ω. The current through the starter motor was not sufficient to rotate it due to the discharge of the battery. Find the current through the starter motor at this instance.
- (h) In the situation mentioned in (g) above, the driver used an external battery with an emf $12 \cdot 3 \text{ V}$ and an internal resistance $0 \cdot 02 \Omega$ to jump start the car. For this, the external battery was connected to the discharged battery using two jumper cables, each having a resistance of $0 \cdot 015 \Omega$ and the car was then started.
 - (i) Draw the circuit diagram showing the connections to the external battery with the discharged battery, when jump starting the car.
 - (ii) Calculate the maximum current through the starter motor when starting the engine.

9. (Part A)

a) Electromotive Force (EMF) = Work Done/Charge

(i)
$$E = \frac{W}{q}$$

Units J

(ii) Work done W = Eq.....(01) Power generated by the source $P = \frac{W}{t} = E \frac{q}{t}$(01) P = EI(The given definition must be used to award marks) b) Total energy dissipated in the circuit in time t = EIt(01) E = I(R+r) **OR** $I = \frac{E}{R+r}$ \therefore Total energy dissipated in the circuit in time t is $E\left(\frac{E}{R+r}\right)t=\frac{E^2}{(R+r)}t$(01) Alternative Method Total energy dissipated in the circuit in time $t = I^2(R+r)t$(01) $E = I(R + r) \Rightarrow I = \frac{E}{R + r}$ \therefore Total energy dissipated in the circuit in time t is $\left(\frac{E}{R+r}\right)^2 (R+r)t = \frac{E^2}{(R+r)}t$ (c)(i)Apply P = VI for a headlamp $60 = 12 \times I \text{ OR } I = 5 A$(01) Reading of the ammeter = 2I = 10 A(ii) To find the resistance of a headlamp use one of the equations below $P = I^2 R$ **OR** $P = \frac{V^2}{R}$ **OR** V = IR $P = I^2 R$ **OR** 60 = 25R.....(01) $R = 2.4 \Omega$(01) (iii) For battery $E = V + Ir = 12 + (10 \times 0.03)$(01) = 12.3 V.....(01) (d) $I_L = 8 A$

 $(i) I = I_L + I_M \to (1)$

$$V = E - Ir \rightarrow (2)$$

$$V = \frac{I_L}{2} r_b \rightarrow (3)$$

$$(3) => V = 4$$

$$(2) = 12.3$$

 $(3) => V = 4 \times 2.4 = 9.6 V$

.....(01)

 $(2) = I = \frac{12.3 - 9.6}{0.03} = 90 A$(01)

 $(1) = I_M = 90 - 8 = 82 A$

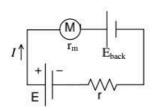
(ii)
$$V = I_M r_m = r_m = \frac{9.6}{82}$$
 (01)

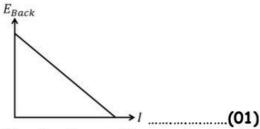
 $= 0.117 \Omega = 0.12 \Omega$(01)

(e) (i) $V^{'}=11.0~V$, $I_{M}^{'}=34.2~A$ $V^{'}=E_{back}+I_{M}^{'}r_{m}$ OR $E_{back}=11-34.2\times0.12=6.90~V\dots$ (No marks allocated) (ii) Efficiency of the stater motor $=\frac{\text{Useful output power}}{\text{Input Power}}\times100~\%$

$$\eta = \frac{E_{back} \times I'_{M}}{V' \times I'_{M}} \times 100 = \frac{6.896}{11} \times 100 = 62.7\%$$
 (No marks allocated)

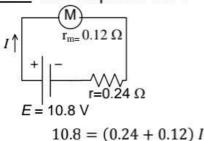
(f)





(For the shape with correct axis only)

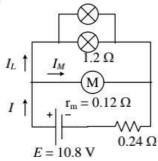
(g) Case I: Head lamps are OFF.



(For the correct substitution)

I = 30 AOR 30.25 A

Case II: The headlamps are kept ON



$$10.8 - (I_L + I_M)0.24 = I_M 0.12$$

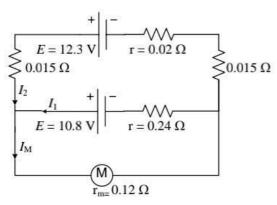
$$10.8 - (I_L + I_M)0.24 = I_L 1.2$$

(For any correct equation).....(01)

Solving above two equations

 $(1) = > 67 + 8 \approx 75 \text{ A}$





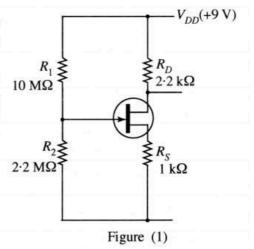
(Positive terminal of discharged battery to positive terminal of external battery should be connected.)

OR 76 A

.....(01)

Part (B)

- (a) (i) Why Field Effect Transistors (FET) are called unipolar devices? What are the charge carriers contributing to the operation of FETs?
 - (ii) State why FETs are also known as voltage-controlled devices.
 - (iii) Calculate the drain current I_D and the Gate-Source voltage V_{GS} for the circuit shown in figure (1), assuming $V_D = 5$ V.



(b) In the Op-amp circuit shown in figure (2), each electromechanical switch S_i (i = 0, 1, 2, 3) is operated by applying an electrical signal D_i (i = 0, 1, 2, 3) which can be 'High' (5V) or 'Low' (0V). When D_i is 'High' the respective switch S_i will be closed and otherwise, it will be open.

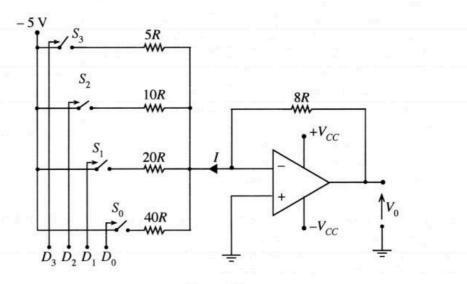


Figure (2)

- (i) When D_2 is 'High', find the current through the resistor 10R in terms of R.
- (ii) If a set of voltages (5 V, 0 V, 5 V, 5 V) is applied simultaneously to operate the switches S_3 , S_2 , S_1 , S_0 , respectively, calculate the current I indicated in figure (2) in terms of R.
- (iii) Calculate the output voltage V_0 when a set of voltages (5 V, 5 V, 5 V, 5 V) is applied simultaneously to operate the switches S_3 , S_2 , S_1 , S_0 , respectively.
- (c) A cash operated snack dispenser will provide a pack of 'Marie' or 'Chocolate Cream' biscuits under the following conditions.
 - The correct amount of cash is inserted (1)
 - 'Marie' (M) or 'Chocolate Cream' (C) is selected
 - If 'Marie' is selected, 'Availability of Marie' in the dispenser (X)
 - If 'Chocolate Cream' is selected, 'Availability of Chocolate Cream' in the dispenser (Y)
 - (i) Obtain the logic expression for the conditions under which a pack of biscuits may be obtained.
 - (ii) Show how this may be implemented using logic gates.

09.(Part B)

(a) (i) Because they operate only with one type of charge carriers(01

Type of charge carriers either electrons or holes

(No Marks for electrons and holes)

(ii) Voltage between two of the terminals (Gate and Source) controls the current through the device(01

(iii) Voltage drop accross the drain resistor R_D

$$V_{DD} - V_D = I_D R_D \implies I_D = \frac{V_{DD} - V_D}{R_D} = \frac{9 - 5}{2 \cdot 2 \times 10^3}$$
(01)

$$I_D = 1.82 \text{ mA}$$
 [1.81 – 1.82 mA](01)

Voltage at source terminal

$$V_S = I_D R_S = (1.82 \times 10^{-3}) \times 1 \times 10^3 = 1.82 \text{ V} [1.81 - 1.82 \text{ V}]$$
(01)

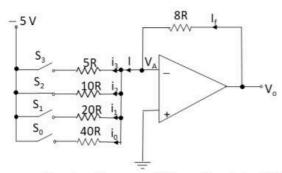
Voltage at gate terminal using potential divider made by R_1 and R_2

$$V_G = \left(\frac{R_2}{R_1 + R_2}\right) V_{DD} = \frac{2 \cdot 2 \times 10^6}{12 \cdot 2 \times 10^6} \times 9 = 1.62 \text{ V}$$
(01)

The Gate-Source Voltage; $V_{GS} = V_G - V_S = 1.62 - 1.82$ (01)

$$= -0.2 \text{ V}$$
 [(-0.19 V) - (-0.20 V)](01)

(b) (i)



According to the conditions for ideal OP-AMP (from the golden rules of OP-AMP) $\Rightarrow V_A = V_- = V_+ = O$ (Since non-inverting terminal is grounded) i.e. point A is at virtual ground

$$i_2 = \frac{V_A \cdot (-5)}{10R} = \frac{0 \cdot (-5)}{10R}$$

$$= \frac{1}{2R}$$
(01)

(ii) According to the conditions for ideal OP-AMP, the current following in to the OP-AMP through the inverting terminal is zero.

By applying Kirchoff's current law to the node at the inverting terminal of OP-AMP

$$I = i_3 + i_2 + i_1 + i_0$$

$$= \frac{0 \cdot (-5)}{5R} + \frac{0}{10R} + \frac{0 \cdot (-5)}{20R} + \frac{0 \cdot (-5)}{40R}$$

$$= \frac{1}{R} + 0 + \frac{1}{4R} + \frac{1}{8R}$$

$$= \frac{11}{4R}$$
(01)

Alternative Method Finding equivalent resistance $\frac{1}{R'} = \frac{1}{5R} + \frac{1}{20R} + \frac{1}{40R} \tag{01}$ $\frac{1}{R'} = \frac{11}{40R} \tag{01}$ $I = \frac{0 - (-5)}{40R/11} = \frac{11}{8R} \tag{01}$

iii) All the switches are closed (as in the same way of part ii)

$$I = i_3 + i_2 + i_1 + i_0$$

$$I = \frac{5}{5R} + \frac{5}{10R} + \frac{5}{20R} + \frac{5}{40R}$$

$$I = \frac{1}{R} + \frac{1}{2R} + \frac{1}{4R} + \frac{1}{8R}$$

Since the current following into the OP AMP through the inverting terminal is zero

| Also $I_f = I$ | (01) |
|---------------------------------------------|------|
| $I_f = \frac{V_o - V_A}{8R}$ | (01) |
| $=\frac{V_o \cdot \theta}{8R}$ | (01) |
| $\therefore \frac{V_o}{8R} = \frac{15}{8R}$ | (01) |
| $V_o = 15 \mathrm{V}$ | (01) |

Alternative method

Since all switches are closed, equivalent resistance of the input side

$$\frac{1}{R'} = \frac{1}{5R} + \frac{1}{10R} + \frac{1}{20R} + \frac{1}{40R}$$

$$\frac{1}{R'} = \frac{15}{40R}$$

$$\therefore R' = \frac{40R}{15}$$
.....(01)

$$\therefore R' = \frac{40R}{15} \tag{O1}$$

Voltage gain of an inverting amplifier =
$$\frac{V_o}{V_{in}} = -\frac{R_f}{R_{in}}$$
(01)

$$V_o = -\frac{8R \times 15}{40R} \times -5$$

$$V_o = 15 \text{ V}$$
(01)

(c) (i)
$$B = I[(MX) + (CY)]$$
(04)

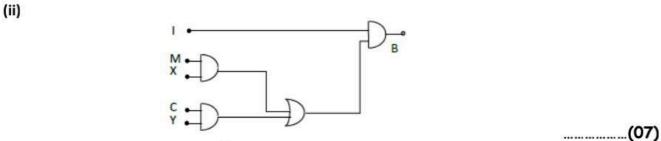
(01 mark each for correct I, MX, CY and + terms)

Alternative Method 1 B = IMX + ICY(01 mark each for correct IMX and ICY terms, and 02 marks for "+" term)

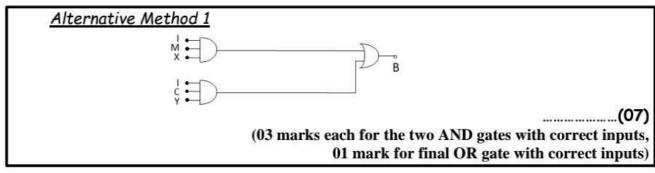
Alternative Method 2

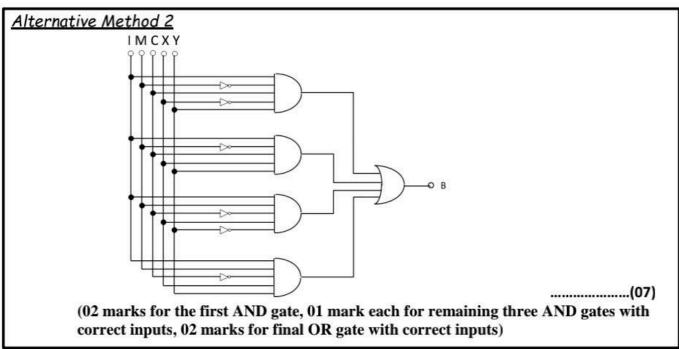
| I | М | С | Х | Υ | В |
|---|---|---|---|---|---|
| 1 | 0 | 1 | 0 | 0 | 0 |
| 1 | 0 | 1 | 0 | 1 | 1 |
| 1 | 0 | 1 | 1 | 0 | 0 |
| 1 | 0 | 1 | 1 | 1 | 1 |
| 1 | 1 | 0 | 0 | 0 | 0 |
| 1 | 1 | 0 | 0 | 1 | 0 |
| 1 | 1 | 0 | 1 | 0 | 1 |
| 1 | 1 | 0 | 1 | 1 | 1 |

(Award for 4 rows with B = 1, 1 mark each for 2 correct rows) B=IMCXY+IMCXY+IMCXY+IMCXY(02)



(02 marks each for 1st two AND gates with correct inputs, 02 marks for OR gate with correct inputs, 01 mark for final AND gate with correct "I" input)





10. Answer either part (A) or part (B) only.

universal gas constant.

Part (A)

- (a) (i) State the Boyle's law and the Charles' law.
 - (ii) Derive the ideal gas equation using the above laws.
- (b) A deflated tyre of volume V and initial pressure P_0 , at room temperature T_R is connected to a compressed nitrogen (N_2) gas tank via a valve. The tyre initially contains only N_2 gas. After inflating the tyre with N_2 gas, its final pressure is P and it contains a total of n number of N_2 moles. Assume that there is no change in volume of the tyre.
 - (i) Assuming that the N_2 gas inside the tyre behaves like an ideal gas, show that the number of moles of N_2 gas pumped into the tyre is $n\left(1-\frac{P_0}{P}\right)$.
 - (ii) Obtain an expression for the work done to inflate the tyre with \boldsymbol{N}_2 gas.
 - (iii) Assuming that the pumping process of N_2 gas is adiabatic, show that the change in the temperature of the N_2 gas inside the tyre is $\frac{2}{5}\left(1-\frac{P_0}{P}\right)T_R$. The change in internal energy of an ideal gas is given by $\Delta U = n \ C_V \ \Delta T$, where C_V is the molar heat capacity at constant volume and ΔT is the change in temperature. The molar heat capacity at constant volume of a diatomic ideal gas is $\frac{5R}{2}$, where R is the
 - (iv) This change in temperature, increases the pressure temporarily to a higher value. Show that this change in pressure is $\frac{2}{5}(P-P_0)$.
- (c) Gauge pressure is the pressure measured relative to atmospheric pressure. Gauge pressure of a tyre is usually expressed in psi (pound per square inch) units. $(1 \text{ atm} \approx 100 \text{ kPa} \text{ and } 1 \text{ psi} \approx 7 \text{ kPa})$

A deflated tyre at 20 psi pressure is pumped further with N_2 gas to a pressure of 30 psi at room temperature (27° C).

- (i) Calculate the change in temperature of N2 gas in the tyre.
- (ii) Calculate the maximum pressure in the tyre due to this change in temperature.
- (iii) Usually this temporary increase in pressure is not observable when pumping N₂ gas further to a deflated tyre. Give two possible reasons for not observing the increase in pressure.

10. Part (A)

(a) (i) Boyle's law

The pressure of a given mass of a gas is inversely proportional to its Volume provided that the temperature remains constant

OR

P $\propto \frac{1}{V}$ for a given mass of the gas at constant temperature, where V & P are volume and pressure of the gas, respectively.

OR

PV = constant for a given mass of the gas at constant temperature, where V & P are volume and pressure of the gas, respectively.

Charles' law

The volume of a given mass of the gas is directly proportional to its absolute temperature, provided that the pressure remains constant.

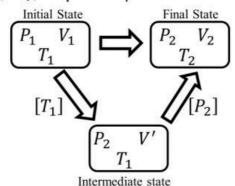
OR

 $V \propto T$ for a given mass of the gas under a constant pressure, where V & T are volume and absolute temperature of the gas, respectively.

OR

 $\frac{V}{T}$ = constant for a given mass of the gas under a constant pressure, where V & T are volume and absolute temperature of the gas, respectively.(02)

(ii) Consider one mole of a gas going through the following two stage processes with the initial and final values of the volume, pressure and absolute temperature are (V_1, P_1, T_1) and (V_2, P_2, T_2) , respectively.



Applying Boyle's law for the constant temperature process

$$P_1V_1 = P_2V'$$
 -----(A)(01)

Applying Charles' law for the constant pressure process

$$\frac{V'}{T_1} = \frac{V_2}{T_2}$$
 -----(B)

(A) & (B)
$$\Rightarrow \frac{P_1 V_1}{T_1} = \frac{P_2 V_2}{T_2} \Rightarrow \frac{PV}{T} = \text{constant},$$
(01)

For one mole of gas, the constant is known as the universal gas constant R.

$$\frac{PV}{T} = R$$
 for one mole of gas.(01)

If there are n mole of gas,
$$\frac{PV}{T} = nR$$
(01)

$$PV = nRT$$

(b) (i) Let n_0 be the number of moles of the air in the type at pressure P_0 at T_R

$$n_0 = \frac{P_0 V}{RT_R}$$
(02)
 $n = \frac{PV}{RT_R}$ (02)

$$n = \frac{PV}{RT_P} \tag{02}$$

Number of moles of the air from the tank to the tyre

$$n' = n - n_0 = \frac{PV}{RT_R} - \frac{P_0V}{RT_R}$$

$$= \frac{V(P - P_0)}{RT_R}$$

$$= n\left(\frac{P - P_0}{P}\right)$$

$$= n\left(1 - \frac{P_0}{P}\right)$$
.....(01)

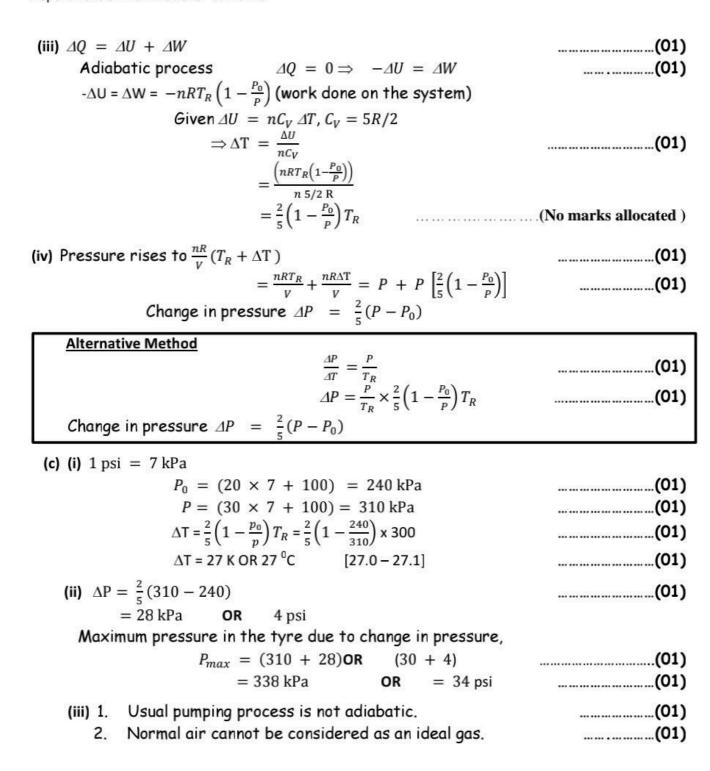
(ii) Let V' be the volume of these n' moles of air in the tank under pressure P_c at temperature T_R

$$V' = \frac{n'RT_R}{P_C} = \left(1 - \frac{P_0}{P}\right) \frac{nRT_R}{P_C}$$

As N2 gas flows from the tank into the tyre through the valve, the tank does work at constant pressure P_C given = P_CV'(01)

(Award this mark for identifying the work as $P \Delta V$)

$$= nRT_R \left(1 - \frac{P_0}{P}\right)$$
(No marks allocated)



Part (B)

Read the following passage and answer the questions.

Radioactivity is a spontaneous decay process by which an unstable nucleus becomes a stable nucleus by emitting radiation. Decay rate is directly proportional to the number of radioactive atoms present at that instant but independent of external physical conditions.

Radioactive iodine 131 I is used in nuclear medicine to treat patients with thyroid cancer. The half-life time of 131 I is 8 days. It decays to stable 131 Xe initially by emitting a β^- particle and then by emitting a γ -photon. The maximum tissue penetration length of this β^- is 2 mm. Usually 131 I is administered to patients as sodium iodide (Na 131 I) in the form of a capsule. Once administered, it is absorbed into the blood stream and concentrated in the thyroid gland. Radiation emitted from 131 I kills most of the cancer cells in the thyroid gland.

Since the patient becomes a potential source of radiation, precautions must be taken to minimize the radiation exposure to others around. The amount of radiation emitted by the patient is proportional to the activity of the dose administered. In medical practice, the common unit used for activity is Curie (Ci) which is not an SI unit. One Curie is equal to 37×10^9 disintegrations per second.

A radioactive material inside the body, diminishes not only by radioactive decay but also by biological clearance. This clearance is purely a biological process and follows an exponential variation, characterized by the decay constant λ_b . Hence the effective decay constant λ_e , due to both radioactive decay and biological clearance can be stated as $\lambda_e = \lambda_p + \lambda_b$, where λ_p is the decay constant corresponding to physical radioactive decay. The effective half-life time, which is used for radiation protection measures, is calculated from the effective decay constant.

- (a) (i) State **two** differences between the emissions of β^- and γ .
 - (ii) Rewrite the following decay equation replacing a, b, and c with correct numbers.

$$^{131}_{53}I \longrightarrow ^{131}_{a}Xe + {}^{b}_{c}\beta^{-}$$

- (b) A fresh sample of Na¹³¹I, having an activity of 100 mCi is received by a hospital. The sample is stored in a lead container at room temperature.
 - (i) What is the SI unit used for activity?
 - (ii) Write down an expression for the decay constant λ in terms of half-life time T.
 - (iii) Calculate the activity of the above sample after 4 days and express the answer in SI units. (Take $\ln 2 = 0.7$ and $e^{-0.35} = 0.7$)
 - (iv) Hence, express the change in activity as a percentage.
 - (v) Is it possible to reduce the activity of the Na¹³¹I sample if it is stored at 0°C instead of storing at room temperature? Explain the answer.
- (c) A small amount of Na¹³¹I sample having an activity of 100 mCi is administered to a thyroid patient.
 - (i) When dealing with such a patient, for which mode of emission, the radiation protection measures should be taken? Explain the answer.
 - (ii) Show that the effective half-life time T_e of $^{131}{\rm I}$ in thyroid gland can be given by $\frac{1}{T_e} = \frac{1}{T_p} + \frac{1}{T_b}$, where T_p and T_b are the half-life times due to radioactive decay and biological clearance, respectively.
 - (iii) If the biological half-life time of ¹³¹I in thyroid gland is 24 days, calculate the effective half-life time of ¹³¹I (in days).
 - (iv) Calculate the percentage change in the activity after 4 days of administration of ^{131}I . (Take $e^{-0.46} = 0.63$)
 - (v) According to radiation protection regulations, ¹³¹I treated patients can be discharged from the hospital when the activity is below or equal to 50 mCi. If this regulation is followed, how long the above ¹³¹I treated patient has to be kept in isolation in the hospital before discharging?

10. Part (B)

(a) (i)

| β- | γ |
|--------------------------------------------------------|--------------------------------------------|
| is a particle emission | is a photon/ an electromagnetic radiation. |
| β – emission changes the proton number/ atomic number) | no change in proton number/ atomic number |

(02 Marks for each difference)......(04) (No Marks for properties of β and γ) $^{131}_{53}I \rightarrow ^{131}_{54}Xe + ^{0}_{-1}\beta^{-}$ (ii) a = 54, b = 0, and c = -1(01×3).....(03) (b) (i) Bq (Becquerel)(02) $\lambda = \frac{\ln 2}{T}$ **OR** $\lambda = \frac{0.693}{T}$ **OR** $\lambda = \frac{0.7}{T}$(02) (ii) $A_4 = A_0 e^{-\lambda t}$ (iii) $= 100 \times e^{-\frac{0.693}{8} \times 4} = 100 \times e^{-0.35}$ $= 70 \, \text{mCi}$ $= 70 \times 37 \times 10^6 \text{ Bg}$ $= 2.59 \times 10^9 \text{ Bg}$(No marks allocated) Change = $\frac{(100-70)mCi}{100 mCi} \times 100\%$ (iv)(No marks allocated) (v) Radioactivity is independent of external physical conditions.(02) y radiation (c) (i) β^- will not come out of the body as the maximum penetration length is 2 mm. OR y radiation has longer penetration length/Power $\lambda_e = \lambda_p + \lambda_b$ (ii) Since $\lambda = \frac{0.693}{T}$ $\frac{0.693}{T_e} = \frac{0.693}{T_p} + \frac{0.693}{T_b}$(03) Therefore, $\frac{1}{T_e} = \frac{1}{T_n} + \frac{1}{T_h}$ $\frac{1}{T_e} = \frac{1}{8} + \frac{1}{24}$(02) (iii) $T_e = 6 \; \mathrm{days}$ $A_4 = A_0 e^{-\lambda t}$ (iv) $= 100 \times e^{-\frac{0.693}{6} \times 4} = 100 \times e^{-0.46}$ Change = $\frac{(100-63)}{100} \times 100\%$ = 37 %.....(No marks allocated)

Because the effective half lifetime is 6 days.

(v)

6 days

.....(04)